

## **Evolutionary Design and Experimental Validation of a Flexible Caudal Fin for Robotic Fish**

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# Biomutualism



Bio-inspiration

Material properties

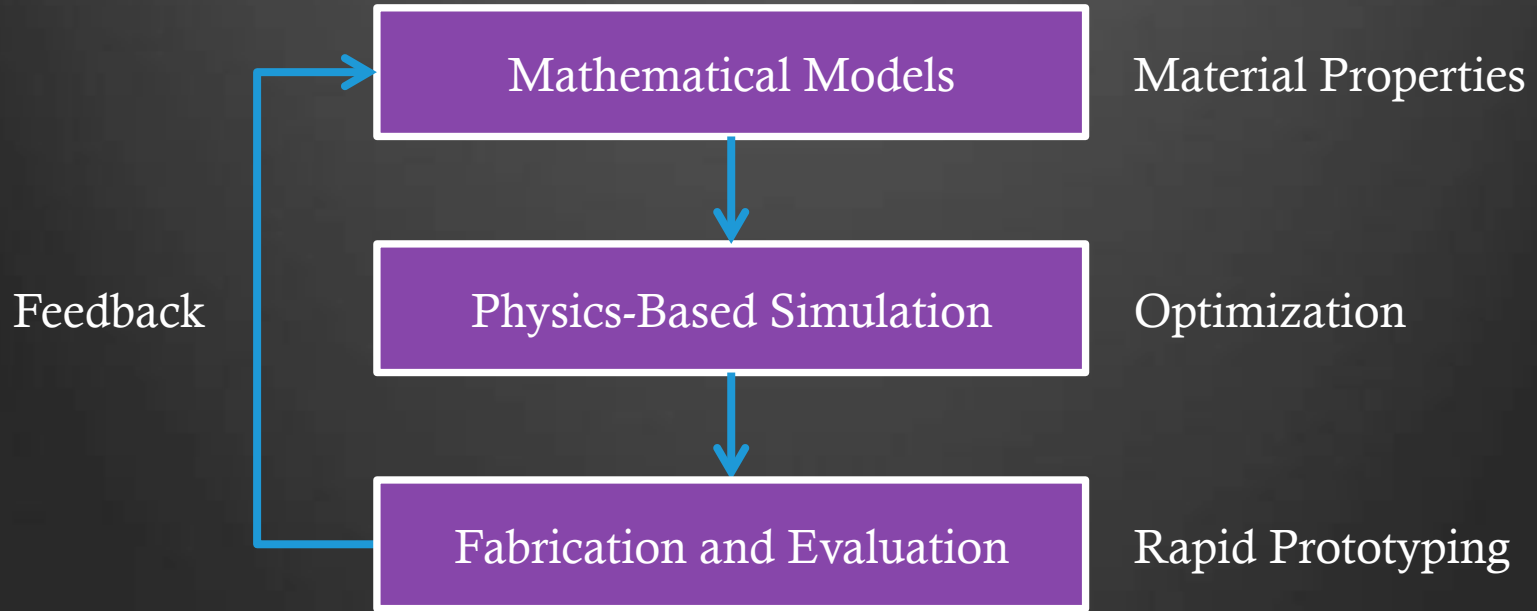
- Passive
- Flexibility



Robotic Fish

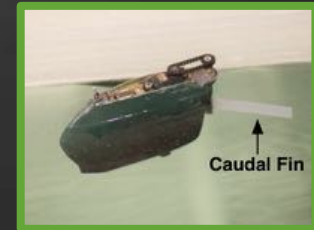
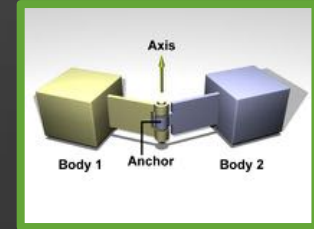
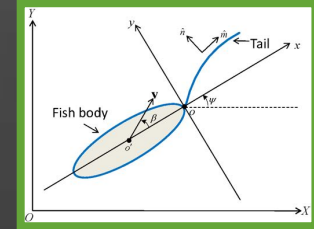
- Evolutionary robotics

# Design Process



# Study Overview

- Optimize Caudal Fin
  - Dimensions
  - Flexibility
- Physically Validate
  - Stable velocity
  - Improve simulation



# Applications

Ecological Monitoring



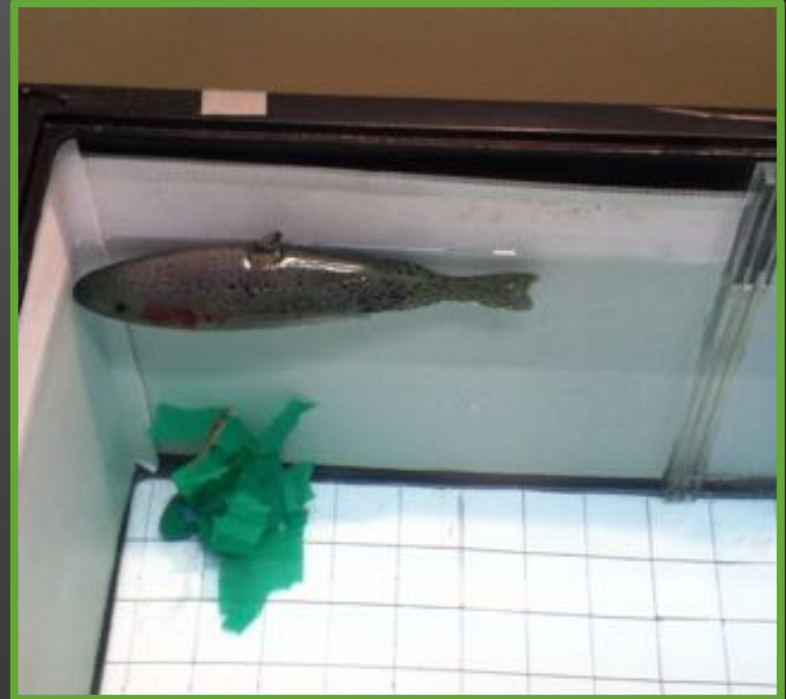
Harbor Surveillance



# Biological Studies

Elicit a response

- ex. robot as predator
  - Predator inspection
- ex. robot as leader
  - Schooling



# Outline

- Introduction
- **Evolution Park**
- This Study
  - Only Flexibility
  - Flexibility + Dimensions
- Conclusion

# Evolution Park

- NSP-Sponsored testbed
- Cross department collaboration
- Facilities
  - Robot grab-bag
  - Compute cluster
  - 4,500 gallon test tank
  - Rapid prototyping 3D printer





# 3D Printer

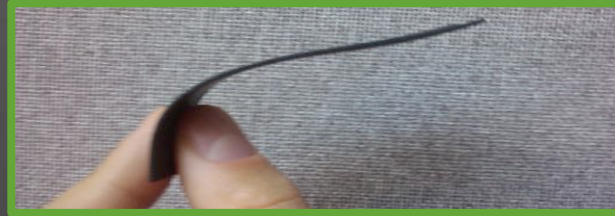
Objet Connex350

Prints multiple material



# Young's Modulus

- (Modulus of elasticity)
- Material property
- Higher value  $\rightarrow$  higher stiffness
- Lower value  $\rightarrow$  higher flexibility



$\sim 0.01$  GPa

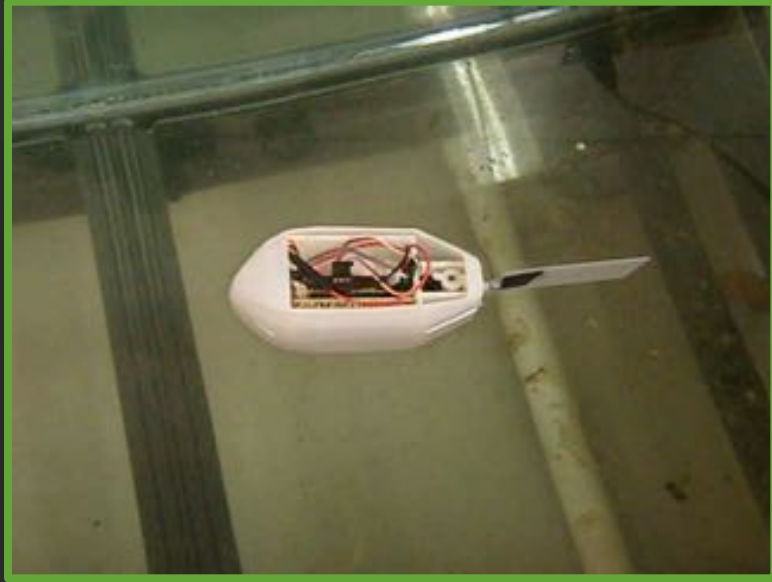


$\sim 10$  GPa



$\sim 100$  GPa

# Printed Robotic Fish



# Printed Robotic Fish

- Printed parts
  - body
  - gears
  - fins
- Electronics
  - Arduino
  - Servo
  - LiPo battery

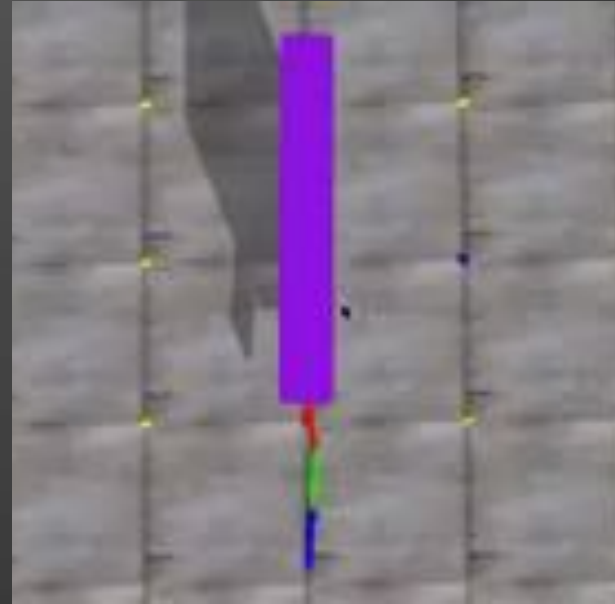


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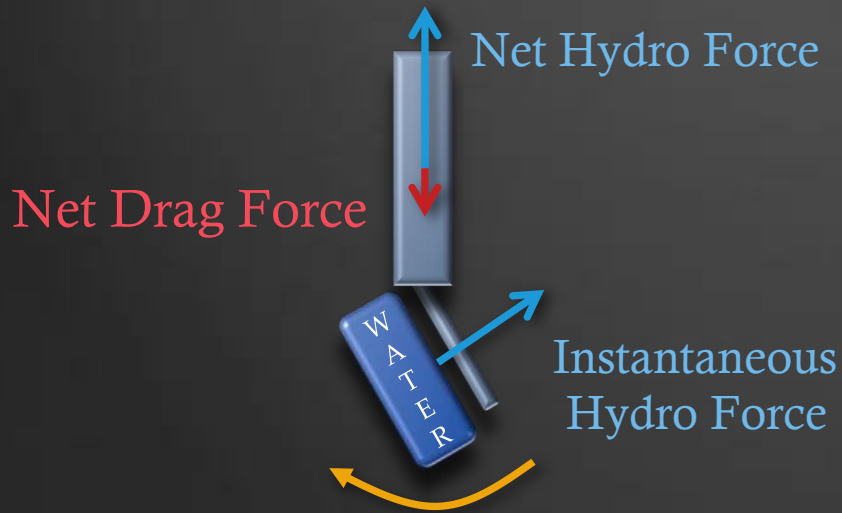
# Study Parameters

- Fixed control
  - 30° amplitude
  - 0.9 Hz frequency
- Flexible, rectangular caudal fin
- Swims on the surface



# Mathematical Model

## Hydrodynamics

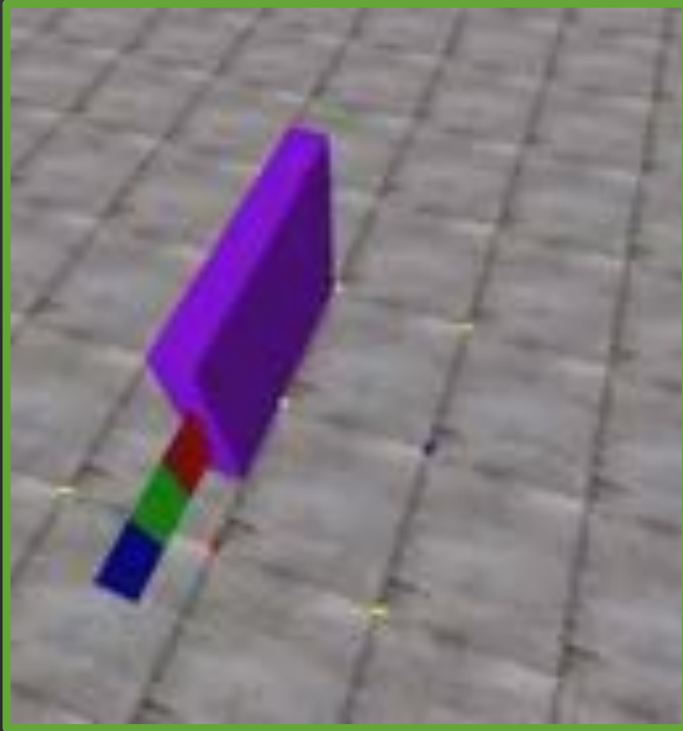


Wang et. al. 2011, 2012

## Flexibility



# Caudal Fin Example





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# Optimize Only Flexibility

## Optimization target

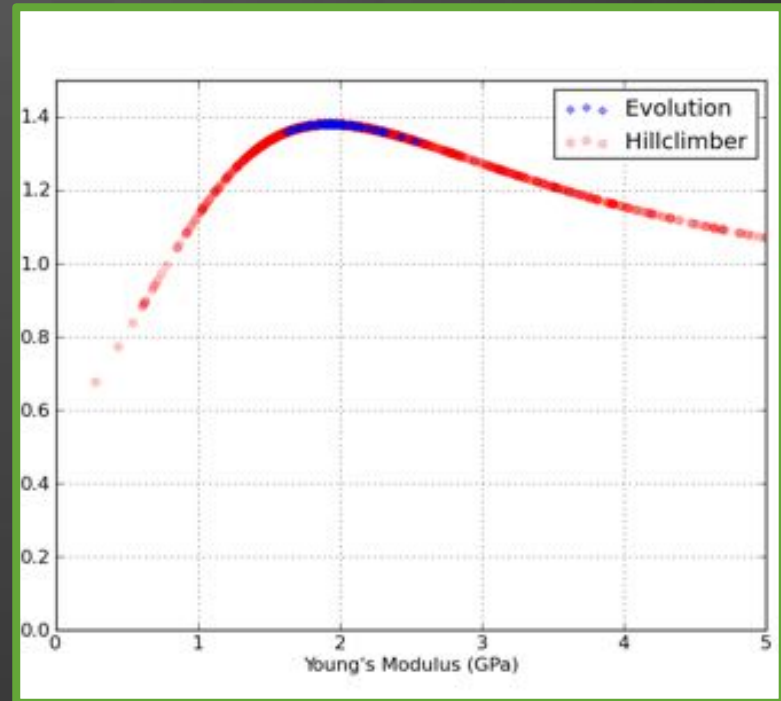
- Maximal average velocity

## Hill-climber

- 30 runs
- 100 candidates tested

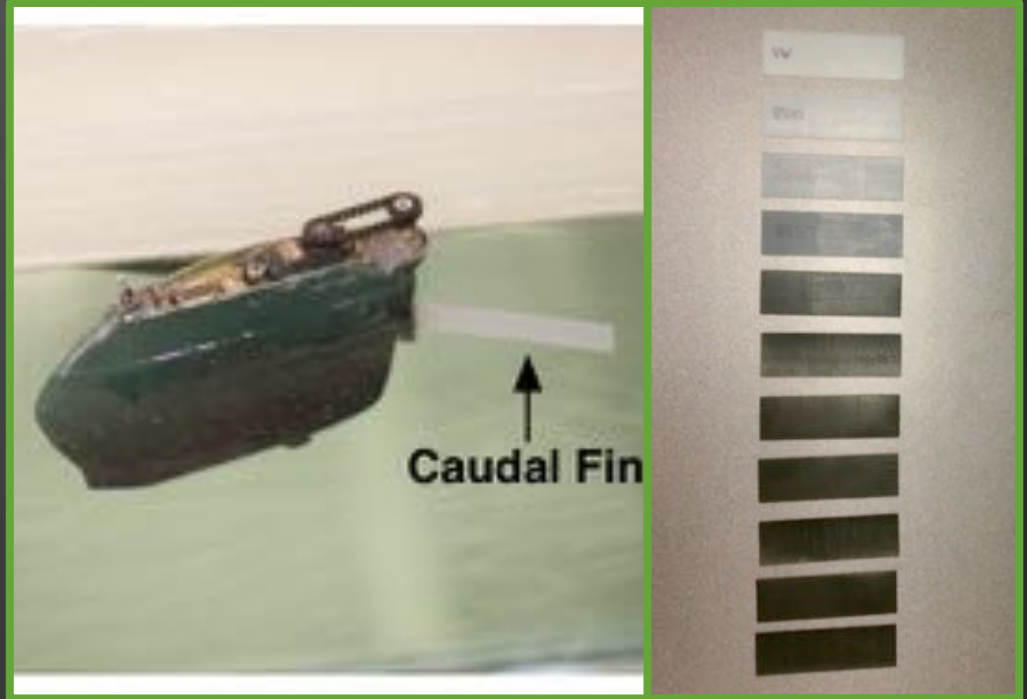
## Evolution

- 30 runs
- 100 individuals
- 100 generations



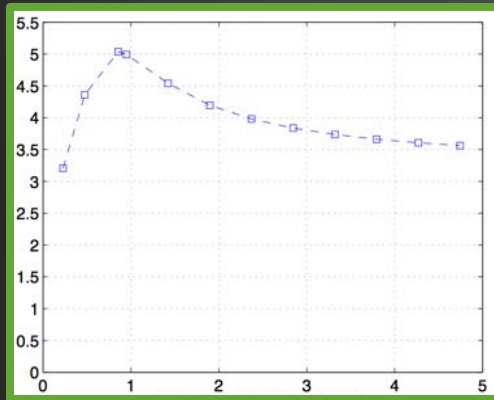
# Physical Validation

- Stable velocity
- Seven trials
  - Remove best
  - Remove worst
  - Compute average

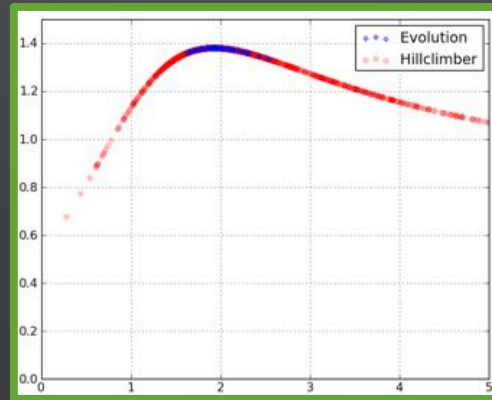


# Experimental Comparison

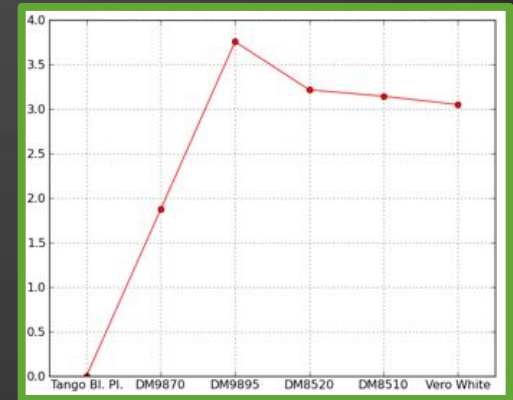
Model Prediction



Simulation Results



3D Printed Materials



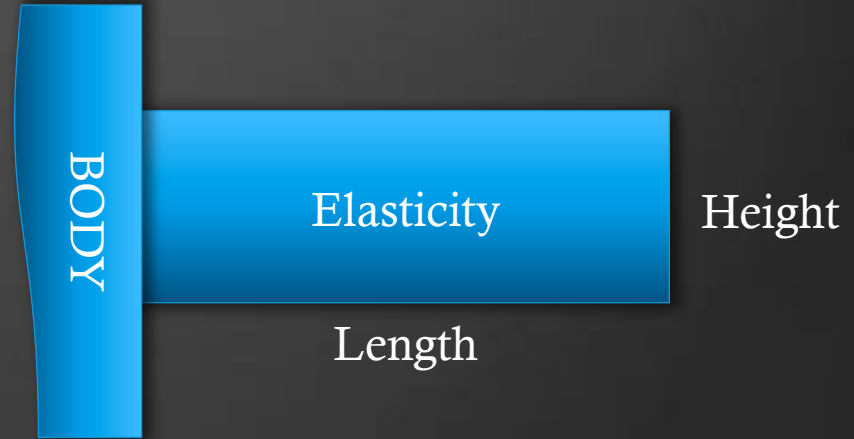
Improved Model

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# Optimization Dimensions and Flexibility

- Evolve
  - flexibility
  - fin dimensions
- Maximal average velocity



# Optimization Dimensions and Flexibility

- Maximal flexibility for every set of dimensions
- Constraints
  - $\text{Length}_{\max} = 14 \text{ cm}$
  - $\text{Length}_{\min} = 4 \text{ cm}$
  - $\text{Modulus}_{\max} = 50 \text{ GPa}$



# Conclusion

- For **E**volutionary **C**omputation
  - Models can approximate flexible materials
  - Models can approximate hydrodynamics
  - Multi-material 3D printers can fabricate evolved flexible solutions
- **EC** results can help improve the modeling process
- Design process can be repeated for other environments



# Future Directions

- Energy consumption
- Morphology
  - Expand models
  - Non-rectangular fins
- Complex tasks
  - Speed, maneuverability
  - Higher level → waypoint following

# Acknowledgements

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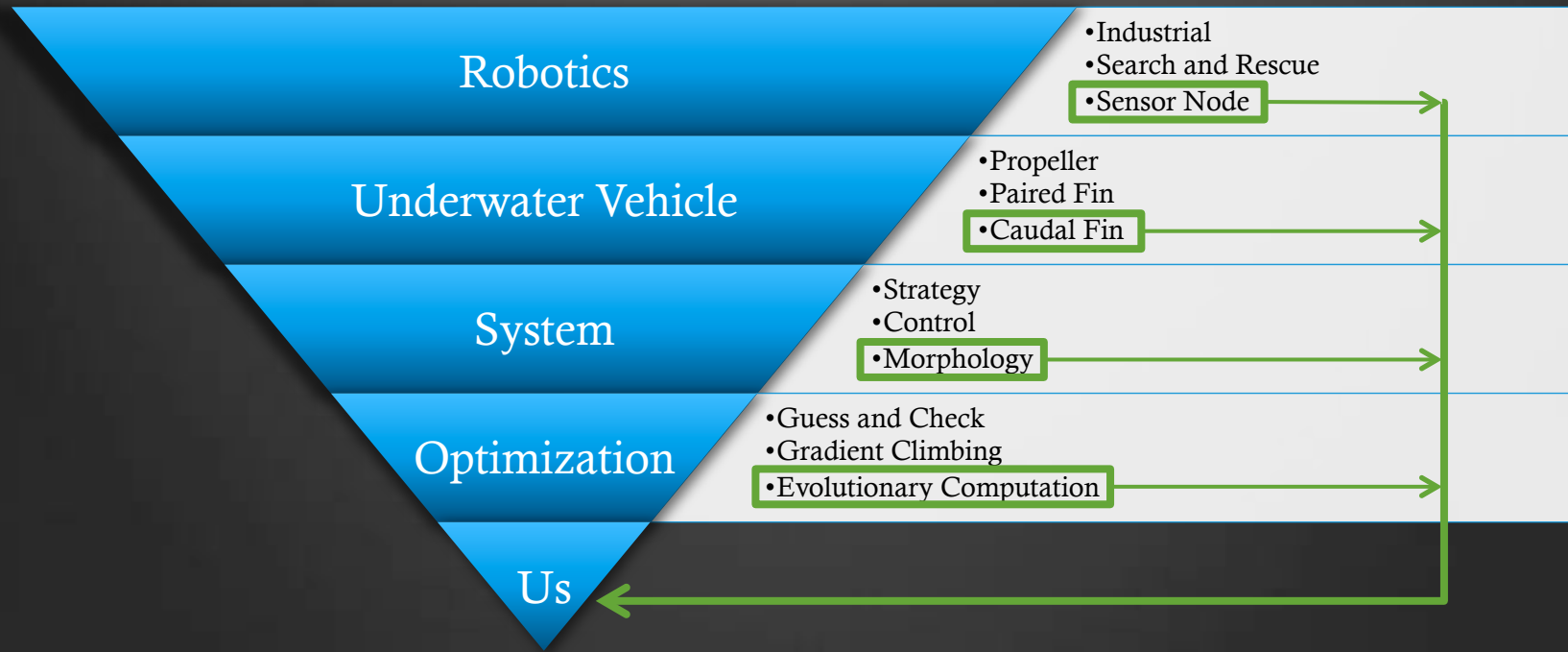
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thank you



# Big Picture



# Mathematical Model

- Aquatic environment
  - Reality gap
  - Model accuracy
- Elongated-body theory

$$\vec{f}(\tau) = \begin{pmatrix} f_X(\tau) \\ f_Y(\tau) \end{pmatrix} = -m \frac{d}{dt}(v_{\perp} \hat{n}), \quad (1)$$

$$\vec{F}_L = \begin{pmatrix} F_{LX} \\ F_{LY} \end{pmatrix} = \left[ -\frac{1}{2} m v_{\perp}^2 \hat{m} + m v_{\perp} v_{\parallel} \hat{n} \right]_{\tau=L}, \quad (2)$$

$$K_s = \frac{E d h^3}{12 l}, \quad (3)$$

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# Future Directions

Efficiency

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Power usage

Mechanical work

Performance

Coevolution

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Control

Morphology

Complex tasks



Multi-Objective